## RI. SE **REVIEWING THE RELATIONSHIP BETWEEN INFORMATION AND ENERGY,** AND THE PHYSICAL LIMITS **OF COMPUTATION**

#### Dr Jon Summers

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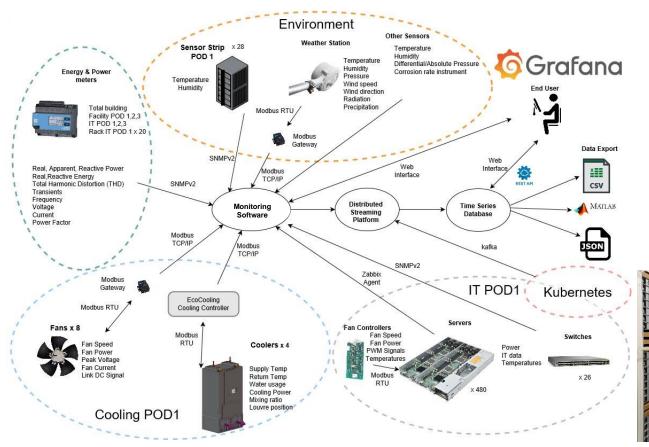
ICT DIVISION, Research Institutes of Sweden PPAM 2019 Bialystok, Poland, September 8-11, 2019



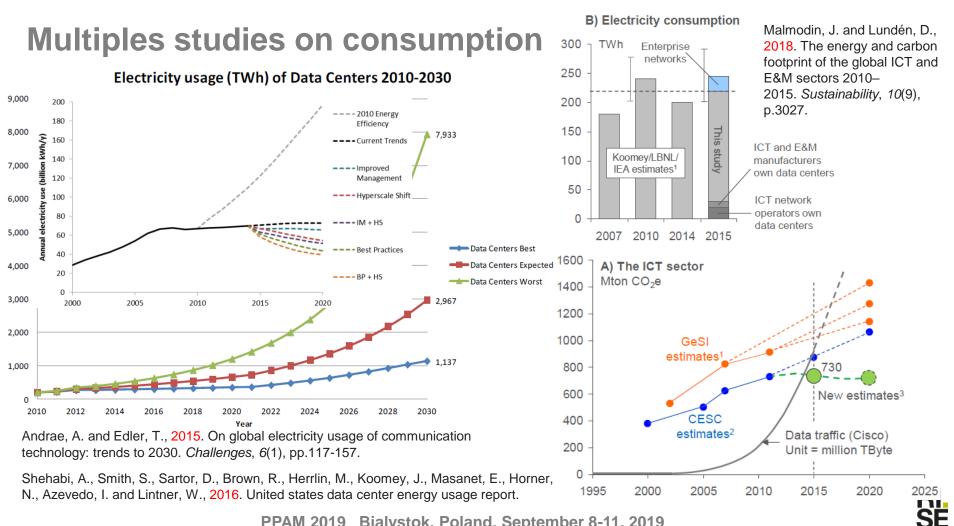




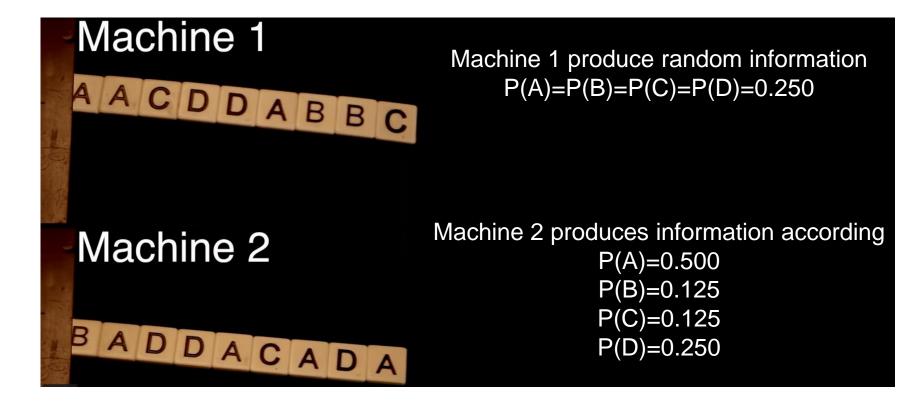
#### **Open source monitoring system**







#### What is information? A quick look back at Shannon



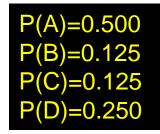


#### Shannon asked how to predict the next symbol

- Machine 1. Ask binary questions. Is it (A or B) or (C or D)? If A or B is YES. Then ask a second binary question. Is it A or B? If B is YES, then the uncertainty of Machine 1 is 2 questions per symbol.
- Machine 2. Ask binary questions. Is it A? If YES then only 1 question. If NO then ask question: Is it D? If YES then we asked 2 questions. If NO then ask question: Is it B or C?



#### How many questions on average?



- Machine 2: Ask 1 question 50% of the time to guess A, 2 questions 25% of the time to guess D, 3 questions 25% of the time to guess B or C. So the average number of questions to ask is:
- #questions = 1 x P(A) + 2 x P(D) + 3 x P(B) + 3 x P(C), which is 1.75 questions per symbol on average.
- So if we need to guess 100 symbols from both machines we would need to ask 200 questions for Machine 1, but 175 questions for Machine 2. Machine 2 is producing less information! Less uncertainty or surprise in its output.



#### Shannon's information entropy

- Claude Shannon called this measure of uncertainty, information entropy, using the symbol H.
- The units of H are based on the uncertainty of a fair coin flip. Shannon used "bit" based on a fair coin flip.

• 
$$H(p_1, p_2, \dots, p_n) = \sum_i p_i \times #questions_i$$

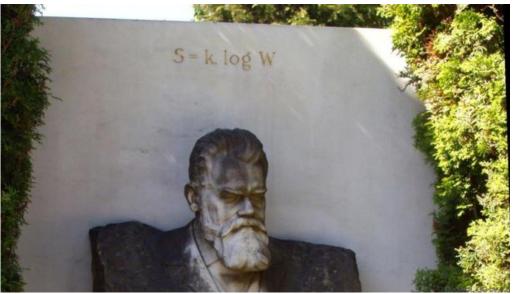
• #questions<sub>i</sub> = 
$$log_2$$
(#outcomes) =  $log_2\left(\frac{1}{p_i}\right)$ 

$$H(p_1, p_2, \dots, p_n) = -\sum_i p_i \log_2(p_i)$$

#### **Boltzmann (thermodynamic) Entropy**

 In terms of a dilute gas the "thermodynamic" entropy, *S*, is written as *S* = k<sub>B</sub>lnW where *W* is the number of real microstates of the gas

In statistical mechanics,



a microstate is a specific microscopic configuration of a thermodynamic system that the system may occupy with a certain probability in the course of its thermal fluctuations.



#### **Boltzmann's constant**

- A universal constant that relates a gas molecules kinetic energy to its temperature, so it is measure in J/K – Joules per Kelvin
- The value is 1.380649×10<sup>-23</sup> J/K and is equal to the Universal Gas Constant, *R*, divided by Avogadro's constant, *N<sub>A</sub>*. *R* is the energy required to raise 1 mole of a substance by 1 Kelvin and  $N_A$  is the number of molecules in 1 mole of a substance.
- Energy required to raise 1 molecule by 1 Kelvin.
- So  $S = -k_B \sum_i p_i ln(p_i)$  which reduces to  $S = k_B lnW$  if all probabilities,  $p_i$ , are equal.



#### Maxwell's Demon

- Thought experiment proposed by James Clerk Maxwell in 1867.
- The Demon sorts hot and cold (respectively fast and slow moving) particles
- End up with oven (A) and fridge (B) and no energy **consumed**!
- Contradicts second law of thermodynamics (creating order from disorder – reducing Entropy).
- Does it imply a relationship between information and energy?



#### Szilard's answer

- An attempt to explain the paradox of Maxwell's demon was put forward by Szilard in 1929.
- Szilard argued that there must be an entropic cost associated with the Demon's acquisition of *information*.
- Boltzmann's statistical mechanics definition of entropy involves probability of microstates.
- Therefore an increase in *information* corresponds to a decrease in *entropy*. (Brillouin later used *negentropy*)
- There is still much debate, see the 2015 article "A few exciting words": Information and Entropy revisited.

Szilard, Leo. über die Entropieverminderung in einem thermodynamischen System bei Eingriffen intelligenter Wesen Journal Zeitschrift für Physik Volume 53, Issue 11-12 (1929), pp 840-856.

Brillouin, Leon. "Maxwell's demon cannot operate: Information and entropy. I." Journal of Applied Physics 22.3 (1951): 334-337.

Bawden, David, and Lyn Robinson. ""A few exciting words": Information and entropy revisited." *Journal of the Association for Information Science and Technology* (2015).



#### Information is a physical entity

- Information is physical: writing on stone, printing text in a book difficult to reverse so *thermodynamic entropy* always increases.
- In 1961, Rolf Landauer, while working at IBM proposed that the acquisition of one bit of information through erasure of 0 or 1 required dissipation of at least  $k_B \sum_i p_i ln(p_i)T$  J of energy at a temperature T probabilities of 0 or 1 are  $p_1$  and  $p_2$  and are equal at 0.5.
- In principle this assumed no thermodynamic objection to a logically reversible operation.
- In 2012 a team of French researchers published in Nature experimental verification to support the Landauer principle.



Rolf Landane

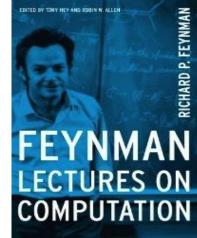
Rolf Landauer (1961), "Irreversibility and heat generation in the computing process", *IBM Journal of Research and Development* **5** (3): 183–191 Antoine Bérut; Artak Arakelyan; Artyom Petrosyan; Sergio Ciliberto; Raoul Dillenschneider; Eric Lutz (8 March 2012), "Experimental verification of Landauer's principle linking information and thermodynamics", *Nature* **483** (7388): 187–190

### **Information and Energy**

- Of course, there are critics such as Norton who identifies thermal fluctuations as a missing component of Landauer's argument
- Rolf Landauer demonstrated that the minimum dissipation of energy in the erasure of 1 bit of information is 2.9zJ (z = Zepto = = 10<sup>-21</sup>) at 300K (27<sup>o</sup>C).
- Bennett's digital tape machine as discussed in Feynman's Lectures on Computation shows that at room temperature a tape carrying a full fuel load, 2.9zJ per bit, carries zero information.
- Could this value of 2.9zJ per bit be a physical limit of computation?

**Norton**, John D. "Waiting for landauer." *Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics* 42.3 (2011): 184-198.

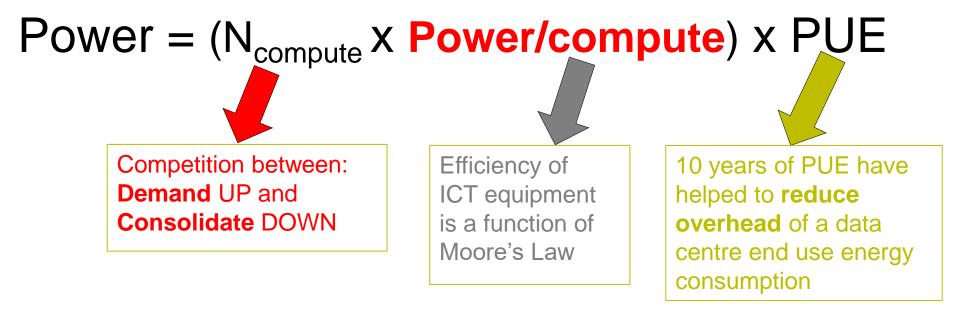
Bennett, C.H., 1982. The thermodynamics of computation—a review. International Journal of Theoretical Physics, 21(12), pp.905-940.





#### Data centre power consumption

Consider the contributing factors to Data Centre Power Consumption:





#### **Power consumption of IT hardware**

# **Power/compute** = $N_{tr} \times Freq \times E_{tr} \times CompUE$

Number of transistors per datacom has increased for 50 years doubled ever 2 years by Moore's law and indicates performance. Clock speeds have not really increased since 2005 as it has a significant effect, but is now variable.

Energy consumption per transistor is key to total power consumption. Compute Usage Effectiveness Overhead from power supply, xDD, RAM, etc.

#### **Note also that** Power/compute = $\alpha \mathbf{x} \mathbf{C} \mathbf{x} \mathbf{V}^2 \mathbf{x}$ Freq + leakage



#### **Energy consumption of a transistor**

Energy/Entropy Factor related to the approach of state changes in Field Effect Transistors (FETs): Depends on Voltage and materials.

Physical constant used statistical mechanics, called the Boltzmann constant with a value of 1.38 x 10<sup>-23</sup> J/K

 $E_{FACTOR}$  X (  $k_{B}$ 

Temperature at which the transistor is operating.

X T)



Summary of relationship of E<sub>FACTOR</sub> with Data Center Power

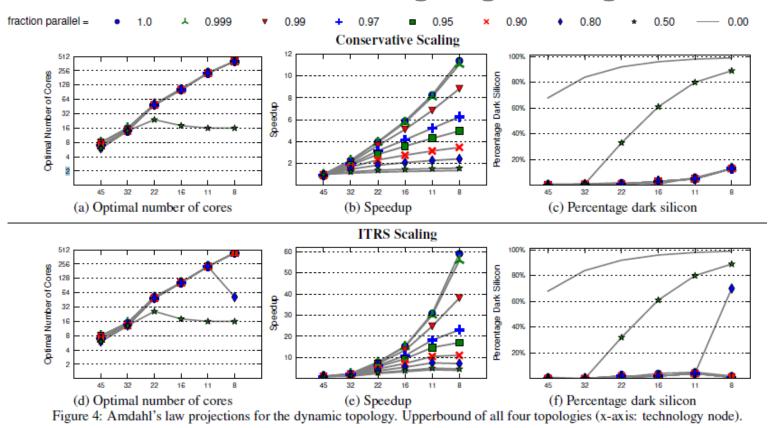
# **<u>Power</u>** = (N<sub>compute</sub> x **Power/compute)** x PUE

## **Power/compute** = $N_{tr} \times Freq \times E_{tr} \times CompUE$

# $\mathbf{E}_{tr} = \mathbf{E}_{FACTOR} \times (\mathbf{k}_B \times \mathbf{T})$



#### Effect of multicore and scaling of gate lengths



Esmaeilzadeh, H., Blem, E., Amant, R.S., Sankaralingam, K. and Burger, D., 2011, June. Dark silicon and the end of multicore scaling. In *Computer Architecture (ISCA), 2011 38th Annual International Symposium on* (pp. 365-376). IEEE.

#### Switching Energy up to today.

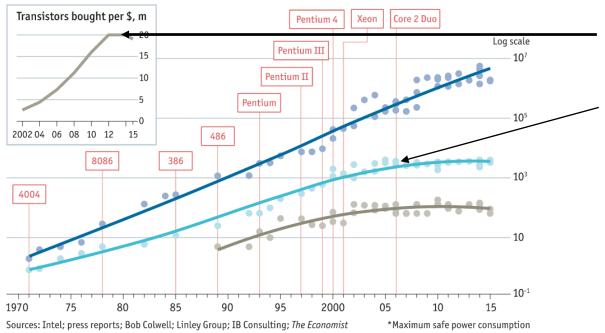
Processor Architecture	Year	Feature Size	Switching Energy (zJ)
Pentium 486	1989	600nm	41137803
Pentium M	2003	130nm	325143
Core	2006	65nm	560819
Nehalem	2008	45nm	156566
Sandy Bridge	2012	32nm	74555Dark
Ivy Bridge	2014	22nm	28994Silcon
Broadwell	2015	14nm	24852 transistors
Intel Xeon Plat 8180	2017	14nm	18743 are
AMD Epyc	2017	14nm	136perational.
Qualcomm Centriq 2400	2018	10nm	10256

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### **E**<sub>FACTOR</sub> is linked to Moore's Law

#### Stuttering

● Transistors per chip, '000 ● Clock speed (max), MHz ● Thermal design power\*, w



Cost of transistors is going up. Peaked at 20 million per \$ in 2015

End of Dennard scaling.

**Moore's Law:** Self-fulfilling prophecy to provide double the number of transistors in the same area every two years.

Cross, T. "After Moore's Law: Double, double, toil and trouble." The Economist, Technology Quarterly, Quarter 1 (2016).

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Chip introduction

dates, selected



## **Getting E<sub>FACTOR</sub> down.**

 millivolt, transistor size and materials may reduce the E<sub>FACTOR</sub>, or going 3D, like gate-all-around.

Waldrop quotes
 "My bet is that we run out of money before we run out of physics"
 [Rock's Law]

Waldrop, M. Mitchell. "The chips are down for Moore's law." *Nature News* 530.7589 (2016): 144.

Carballo, Juan-Antonio, Wei-Ting Jonas Chan, Paolo A. Gargini, Andrew B. Kahng, and Siddhartha Nath. "ITRS 2.0: Toward a re-framing of the Semiconductor Technology Roadmap." In Computer Design (ICCD), 2014 32nd IEEE International Conference on, pp. 139-146. IEEE, 2014.

2015	2017	2019	2021	2024
P70M56	P48M36	P42M24	P32M20	P24M12G1
"16/14"	"11/10"	"8/7"	"6/5"	"4/3"
finFET FDSOI	finFET FDSOI	finFET LGAA	finFET LGAA VGAA	VGAA, M3D
	FinFET	Lateral Nanowire	Vertical Nanowire	Vertical Nanowire
FDSDI	FDSDI	FinFET		Monolithic 3D
28.0	18.0	12.0	10.0	6.0

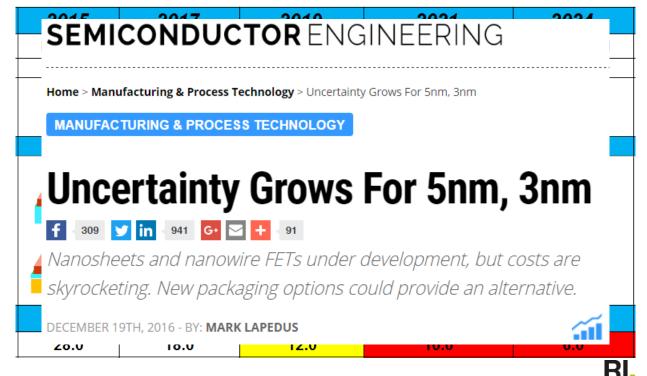
## **Getting E<sub>FACTOR</sub> down.**

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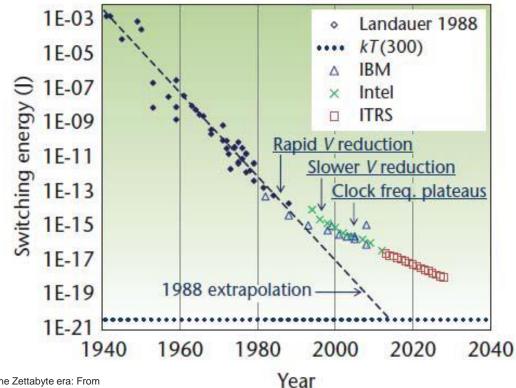


#### **Processing information costs energy.**

1E-17 J is 10,000 zJ and the  $\rm E_{FACTOR}$  is 3,500 today.

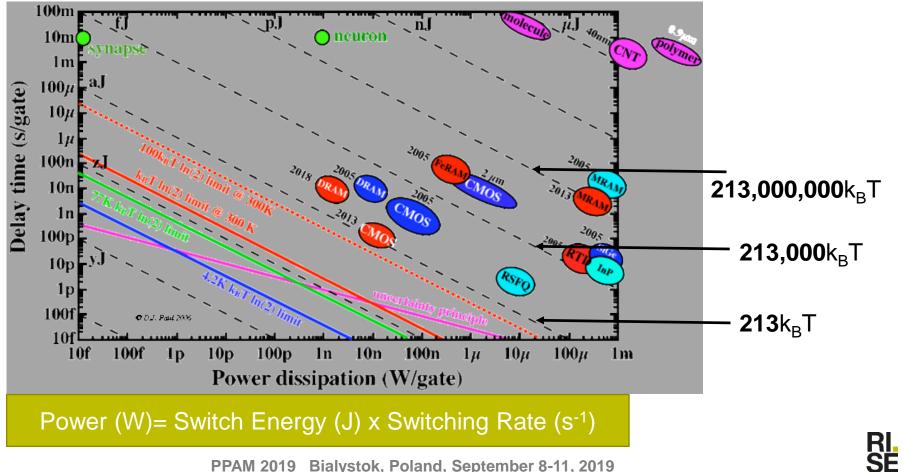
By 2030 the curve shows 1,000 zJ with an  $E_{FACTOR}$  of 350.

Landauer puts the physical limit of  $E_{FACTOR}$  at 0.69.



**Ionescu**, A.M., 2017, December. Energy efficient computing and sensing in the Zettabyte era: From silicon to the cloud. In *Electron Devices Meeting (IEDM), 2017 IEEE International*(pp. 1.2.1-1.2.8). IEEE.

The switching rate is also important



### What are the practical limits of E<sub>FACTOR</sub>?



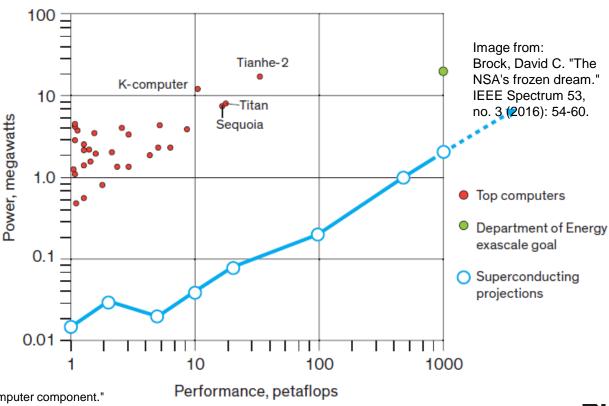
- Frank argues that to measure a signal in the correct state with an error of  $p_e$  (<10<sup>-40</sup>) requires the signal energy to be greater than  $ln(1/p_e)k_BT$ , that is around **100k<sub>B</sub>T**.
- Bennet gave an interesting example of DNA polymerization that occurs in cell division to use  $\sim 40k_BT$  of energy per step.
- If we cannot get E<sub>FACTOR</sub> down, then we reduce temperature, T!

Frank, Michael P. "Approaching the physical limits of computing." *Multiple-Valued Logic, 2005. Proceedings. 35th International Symposium on.* IEEE, 2005.

Bennett, Charles H. "The thermodynamics of computation—a review. "International Journal of Theoretical Physics 21.12 (1982): 905-940.

#### **Superconducting Computing!**

- IBM ran a project from 1973-1983 on this – terminated due to the success of Si.
- At 4K and an E<sub>FACTOR</sub> of 1,500, a cryotron (Buck's superconducting switch) would use 83 zJ and switching frequency of less than 125 THz limited by Planck Constant.



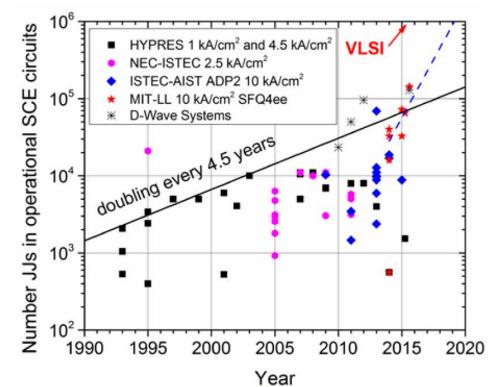
**Buck**, Dudley A. "The cryotron-a superconductive computer component." *Proceedings of the IRE* 44, no. 4 (1956): 482-493.



#### So what about the cryogenics cost?

• A CPU with 5 billion cryotron gates and operating at 3GHz would consume 1.25W of power compared to 160W plus the cryogenics overhead (commercially available use 20kW). BUT

Candidate for 3D.



Tolpygo, Sergey K. "Superconductor digital electronics: Scalability and energy efficiency issues (Review Article)." *Low Temperature Physics* 42, no. 5 (2016): 361-379.



#### **Reversible processes/logic.**

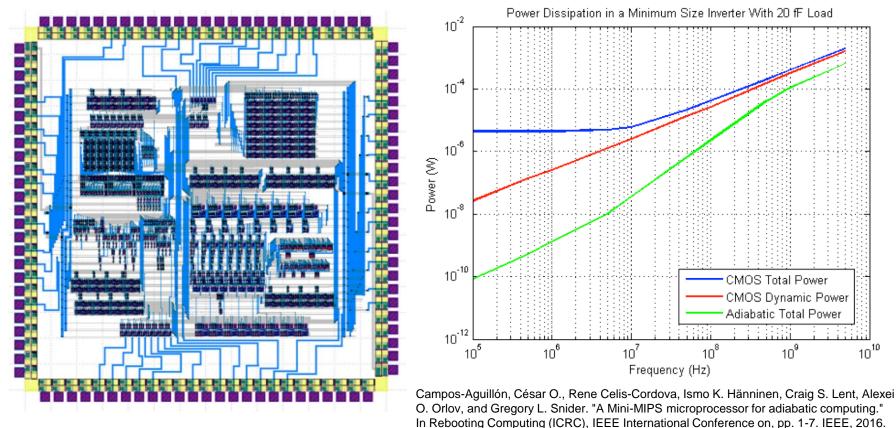
- Computing is logically <u>irreversible</u>, it is not possible to travel backwards through the logic gates and get back to the initial state.
- Bennett, Fredkin, Toffoli, Feynman, Frank and others preset theories behind reversible computing. It is a subject area in its own right.
- Feynman talked about computing through reversible logic gates and then *de-computing* (i.e. reversing the computation), thus not having to dissipate heat on the basis that this would also be physically reversible.

Bennett, C. H. Logical reversibility of computation. IBM J. Res. Dev., 17, 6 (1973), 525-532.
Fredkin, E. F., Toffoli, T. Conservative logic. Int. J. Theo. Phys., 21, 3/4 (1982), 219-253.
Feynman, R. P. Quantum mechanical computers. Found. Phys., 16, 6 (1986), 507-531.
Frank, M. P. (2005, May). Introduction to reversible computing: motivation, progress, and challenges. In *Proceedings of the 2nd Conference on Computing Frontiers* (pp. 385-390). ACM.





#### **Reversible logic**



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#### **Reversible computing**

Snider and workers presented a paper in 2012, which demonstrated experimentally that there is no Landauer limit in computation – they observed a dissipation of 0.04kT < 0.69kT. This was achieved using adiabatically clocked reversible circuits.</li>

Snider, G.L., Blair, E.P., Thorpe, C.C., Appleton, B.T., Boechler, G.P., Orlov, A.O. and Lent, C.S., 2012, August. There is no Landauer Limit: Experimental tests of the Landauer principle. In *Nanotechnology (IEEE-NANO), 2012 12th IEEE Conference on* (pp. 1-6). IEEE.



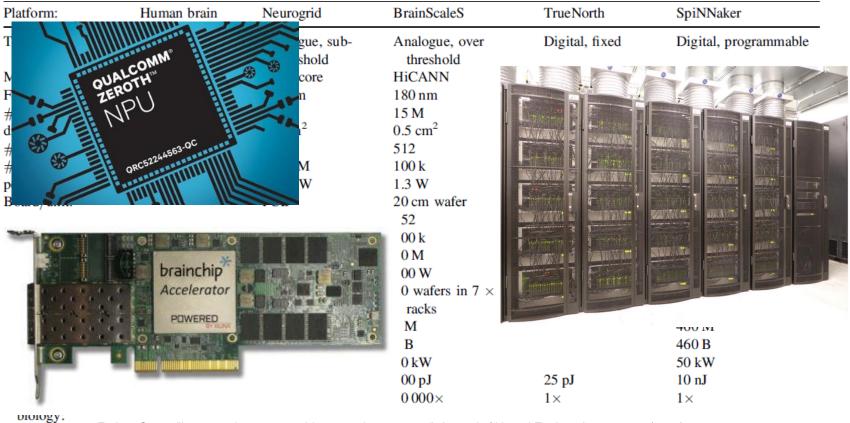
#### **Neuromorphic computing**

Platform:	Human brain	Neurogrid	BrainScaleS	TrueNorth	SpiNNaker
Technology:	Biology	Analogue, sub- threshold	Analogue, over threshold	Digital, fixed	Digital, programmable
Microchip:		Neurocore	HiCANN		18 ARM cores
Feature size:	$10 \ \mu m^{a}$	180 nm	180 nm	28 nm	130 nm
# transistors:		23 M	15 M	5.4 B	100 M
die size:		$1.7 \mathrm{cm}^2$	$0.5 \text{ cm}^2$	$4.3  {\rm cm}^2$	$1 \text{ cm}^2$
# neurons:		65 k	512	1 M	16 k
# synapses:		$\sim 100 \text{ M}$	100 k	256 M	16 M
power:		150 mW	1.3 W	72 mW	1 W
Board/unit:		PCB	20 cm wafer	PCB	PCB
# chips:		16	352	16	48
# neurons:		1 M	200 k	16 M	768 k
# synapses:		4 B	40 M	4B	768 M
power:		3 W	500 W	1 W	80 W
Reference system:	1.4 kg		20 wafers in $7 \times 19''$		600 PCBs in 6 $\times$ 19"
		77 5 4 0 L T	racks		racks
# neurons:	100 B	37,540 k <sub>B</sub> T	4 M		460 M
# synapses:	10 <sup>15</sup>		1 B		460 B
power:	20 W		10 kW		50 kW
Energy/connection:	10 fJ	100 pJ	100 pJ	25 pJ	10 nJ
Speed versus	$1 \times$	1×	10 000×	1×	$1 \times$
biology:	0		a systems " Journal of Noura		(00.10) 051001

Furber, Steve. "Large-scale neuromorphic computing systems." Journal of Neural Engineering 13, no. 5 (2016): 051001.

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#### **Neuromorphic computing**



Furber, Steve. "Large-scale neuromorphic computing systems." Journal of Neural Engineering 13, no. 5 (2016): 051001.

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#### What technology will do the computing of the future?

- CMOS with millivolt, reduce feature size, going 3D and using new materials (error rate, gate-all-around, leakage/quantum effects, heat issue, EUV, new materials still in the lab) [E<sub>tr</sub> = 100k<sub>B</sub>T]
- Superconducting (switch count per unit volume too low)  $[E_{tr} > h/(t_{delay})]$
- Quantum (problem specific, still the challenge of error correction)  $[E_{tr} > h/(t_{delay})]$
- Reversible (complex logic) [ E<sub>tr</sub> = 0.04k<sub>B</sub>T]
- Dark silicon/multicore (software development needed) [ N<sub>tr</sub> < N<sub>tr</sub> ]
- Approximate computing (specialised application) [low bit operations]
- Neuromorphic (potential energy efficiency issues, application specific and massively parallel)



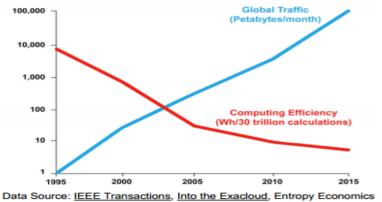
# Store, transmit and compute digital information bottom up approach for 2030

- Battle between digital growth and energy efficiency of compute, storage and transmission of digital information.
- Xu based on Hilbert and Lopez:

Communi-

Year

Storage



#### Computing Energy Efficiency & Total Global Digital Traffic

Special-Purpose<br/>ComputingXu ZW. Cloud-sea computing systems: Towards thousand-fold<br/>improvement in performance per watt for the coming Zettabyte era.<br/>JOURNAL OF COMPUTER SCIENCE AND TECHNOLOGY 29(2):<br/>177–181 Mar. 2014.

**Hilbert**, M. and López, P., 2011. The world's technological capacity to store, communicate, and compute information. science, 332(6025), pp.60-65.



		cation	Computing	Computing
1986	$21\mathrm{PB}$	$59\mathrm{PB}$	$0.3\mathrm{PIPS}$	$0.44\mathrm{PIPS}$
2007	$277\mathrm{EB}$	$537\mathrm{EB}$	$6.39\mathrm{EIPS}$	$189\mathrm{EIPS}$
2030	$140\mathrm{ZB}$	$272\mathrm{ZB}$	$18\mathrm{ZIPS}$	$2570\mathrm{ZIPS}$

General-Purpose

#### SUMMARY

- We do need better predictions of the future of energy consumption by the microelectronics infrastructure, but this depends on what is next for the core technology.
- Clear that the way that we do computation has reached an exciting point. One such individual from the Rebooting Computing project did say "the semiconductor industry has been boring for the last 40 years, it is not getting interesting!"
- Whilst a focus on energy consumption of the devices and infrastructure is important, perhaps even more important for the future is the consumption of resource and material, such as rare earth metals.
- As well as the core data centres and supercomputing centres, more energy is consumed by the digital networks and with 5G poised to grow, future network energy consumption needs to be checked.
- Reduce digital profligacy and increase digital sobriety.

